

WasmBounds

Eliminating Memory Bounds Checks with Abstract Interpretation

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Why do we need a tool to eliminate memory bounds checks?

In Wasm 1.0, OOB accesses are efficiently caught using virtual memory/guard pages.

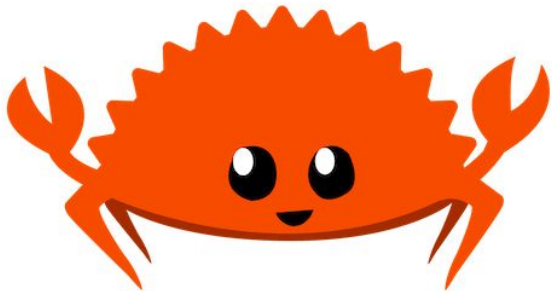


With 64-bit Memory, Single-Byte Page Size, and Embedded Systems, software bounds checking is often used at a cost.

```
if base + offset > length of memory:  
    trap()
```

Wait! We already know that some accesses are safe.

For example, safe languages are already bounds checking accesses to container types.



It's clear at the source level that the accesses are safe...

```
const int N = 1024;

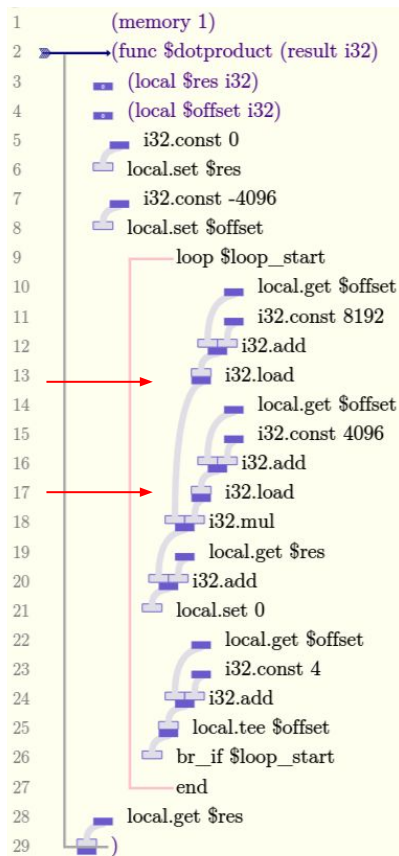
int first[N];
int second[N];

int get_first(int n) {
    return first[n % N];
}

int get_second(int n) {
    return second[n % N];
}

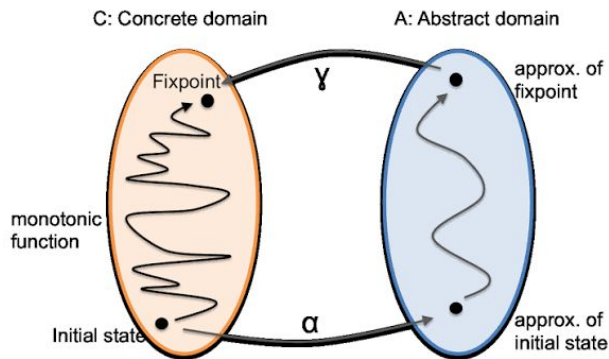
int dotproduct(void) {
    int ret = 0;
    for (unsigned int i = 0; i < N; ++i) {
        ret += get_first(i) * get_second(i);
    }
    return ret;
}
```

...but it's less obvious at the Wasm binary level



We can use abstract interpretation to over-approximate the addresses and eliminate the associated bounds check for provably safe accesses.

1. Translate each Wasm instruction to operate over an abstract domain (strided, sign-agnostic integer intervals)
2. Run through the program using the abstract interpreter multiple times until the abstract store reaches a fix point.



$\{0, 4, 8, 12\} \rightarrow \text{Interval } \{ \text{lower: } 0, \text{ upper: } 12, \text{ stride: } 4 \}$

$4 < 0, 12 >$

Let's walk through the dot product program:

```
1 (memory 1)
2 (func $dotproduct (result i32)
3   (local $res i32)
4   (local $offset i32)
5   i32.const 0
6   local.set $res
7   i32.const -4096
8   local.set $offset
9   loop $loop_start
10    local.get $offset
11    i32.const 8192
12    i32.add
13    i32.load
14    local.get $offset
15    i32.const 4096
16    i32.add
17    i32.load
18    i32.mul
19    local.get $res
20    i32.add
21    local.set 0
22    local.get $offset
23    i32.const 4
24    i32.add
25    local.tee $offset
26    br_if $loop_start
27  end
28  local.get $res
29 )
```

offset: 0< -4096,-4096>

res: 0<0,0>

Let's walk through the dot product program:

```
1 (memory 1)
2 (func $dotproduct (result i32)
3   (local $res i32)
4   (local $offset i32)
5   i32.const 0
6   local.set $res
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15    i32.const 4096
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18    i32.mul
19    local.get $res
20    i32.add
21    local.set 0
22    local.get $offset
23    i32.const 4
24    i32.add
25    local.tee $offset
26    br_if $loop_start
27  end
28  local.get $res
29 )
```

offset: 0< -4096,-4096>

res: 0<0,0>

offset: 0< -4096,-4096>

res: **T**

Let's walk through the dot product program:

```
1 (memory 1)
2 → (func $dotproduct (result i32)
3   (local $res i32)
4   (local $offset i32)
5   i32.const 0
6   local.set $res
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17    i32.load
18    i32.mul
19    local.get $res
20    i32.add
21    local.set 0
22    local.get $offset
23    i32.const 4
24    i32.add
25    local.tee $offset
26    br_if $loop_start
27  end
28  local.get $res
29 )
```

offset: 0< -4096,-4096>

res: 0<0,0>

offset: 0< -4096,-4096>

res: T

offset: 0< -4092,-4092>

res: T

Let's walk through the dot product program:

```

1  (memory 1)
2  → (func $dotproduct (result i32)
3    (local $res i32)
4    (local $offset i32)
5    i32.const 0
6    local.set $res
7    i32.const -4096
8    local.set $offset
9    loop $loop_start
10     local.get $offset
11     i32.const 8192
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19     local.get $res
20     i32.add
21     local.set 0
22     local.get $offset
23     i32.const 4
24     i32.add
25     local.tee $offset
26     br_if $loop_start
27   end
28   local.get $res
29 )

```

offset: $0 < -4096, -4096 >$

res: $0 < 0, 0 >$

offset: $0 < -4096, -4096 >$

res: T

offset: $0 < -4092, -4092 >$

res: T

offset: $\perp \quad 0 < -4092, -4092 > \cap 0 = \emptyset$

res: $\perp$

Let's walk through the dot product program:

```
1 (memory 1)
2 → (func $dotproduct (result i32)
3   (local $res i32)
4   (local $offset i32)
5   i32.const 0
6   local.set $res
7   i32.const -4096
8   local.set $offset
9   loop $loop_start
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18    i32.mul
19    local.get $res
20    i32.add
21    local.set 0
22    local.get $offset
23    i32.const 4
24    i32.add
25    local.tee $offset
26    br_if $loop_start
27  end
28  local.get $res
29 )
```

$0 \langle -4092, -4092 \rangle .\text{remove}(0) = 0 \langle -4092, -4092 \rangle$

$0 \langle -4096, -4096 \rangle \cup 0 \langle -4092, -4092 \rangle$

$0 \langle 0, 0 \rangle \cup T = T$

offset: $4 \langle -4096, -4092 \rangle$

res: T

offset: $0 \langle -4096, -4096 \rangle$

res: T

offset: $0 \langle -4092, -4092 \rangle$

res: T

offset: $\perp$

res: $\perp$

Let's walk through the dot product program:

```
1 (memory 1)
2 (func $dotproduct (result i32)
3   (local $res i32)
4   (local $offset i32)
5   i32.const 0
6   local.set $res
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19    local.get $res
20    i32.add
21    local.set 0
22    local.get $offset
23    i32.const 4
24    i32.add
25    local.tee $offset
26    br_if $loop_start
27  end
28  local.get $res
29 )
```

Thresholds: [-4096, -1, 0, 4, 4096, 8192]

offset: 4< -4096,-1>

res: T

offset: 0< -4096,-4096>

res: T

offset: 0< -4092,-4092>

res: T

offset: $\perp$

res: $\perp$

Let's walk through the dot product program:

```
1 (memory 1)
2 (func $dotproduct (result i32)
3   (local $res i32)
4   (local $offset i32)
5   i32.const 0
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21    local.set 0
22    local.get $offset
23    i32.const 4
24    i32.add
25    local.tee $offset
26    br_if $loop_start
27  end
28  local.get $res
29 )
```

offset: 4< -4096,-4>

res: T

offset: 0< -4096,-4096>

res: T

offset: 0< -4092,-4092>

res: T

offset: $\perp$

res: $\perp$

Let's walk through the dot product program:

```
1 (memory 1)
2 (func $dotproduct (result i32)
3   (local $res i32)
4   (local $offset i32)
5   i32.const 0
6   local.set $res
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8   local.set $offset
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21    local.set 0
22    local.get $offset
23    i32.const 4
24    i32.add
25    local.tee $offset
26    br_if $loop_start
27  end
28  local.get $res
29 )
```

offset: 4< -4096,-4>

res: T

offset: 4< -4096,-4>

res: T

offset: 0< -4092,-4092>

res: T

offset: $\perp$

res: $\perp$

Let's walk through the dot product program:

```
1 (memory 1)
2 (func $dotproduct (result i32)
3   (local $res i32)
4   (local $offset i32)
5   i32.const 0
6   local.set $res
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22    local.get $offset
23    i32.const 4
24    i32.add
25    local.tee $offset
26    br_if $loop_start
27  end
28  local.get $res
29 )
```

offset: 4< -4096,-4>

res: T

offset: 4< -4096,-4>

res: T

offset: 4< -4092, 0>

res: T

offset: $\perp$

res: $\perp$

Let's walk through the dot product program:

```
1 (memory 1)
2 (func $dotproduct (result i32)
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4   (local $offset i32)
5   i32.const 0
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22    local.get $offset
23    i32.const 4
24    i32.add
25    local.tee $offset
26    br_if $loop_start
27  end
28  local.get $res
29 )
```

offset: 4< -4096,-4>

res: T

offset: 4< -4096,-4>

res: T

offset: 4< -4092, 0>

res: T

$4<-4092, 0> \cap 0 = 0$

offset: 0<0, 0>

res: T

Let's walk through the dot product program:

```
1 (memory 1)
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4   (local $offset i32)
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6   local.set $res
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18    i32.mul
19    local.get $res
20    i32.add
21    local.set 0
22    local.get $offset
23    i32.const 4
24    i32.add
25    local.tee $offset
26    br_if $loop_start
27  end
28  local.get $res
29 )
```

$4 < -4092, 0 > .\text{remove}(0) = 4 < -4092, -4 >$

Fix point!

offset: $4 < -4096, -4 >$

res: T

offset: $4 < -4096, -4 >$

res: T

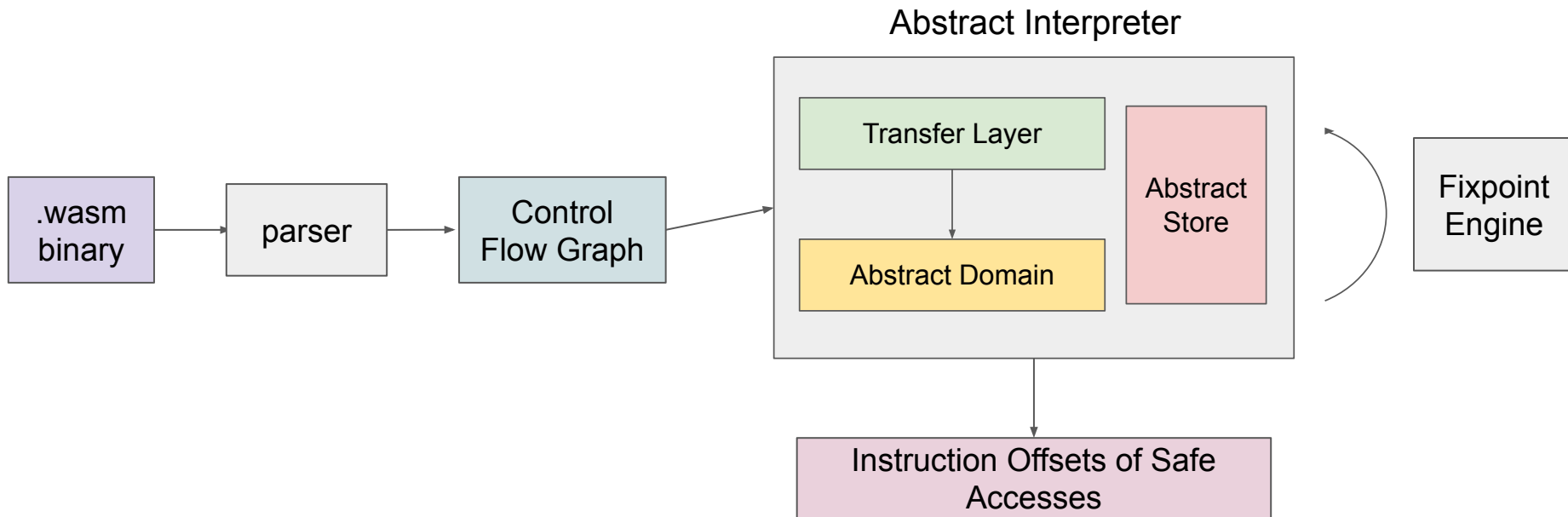
offset: $4 < -4092, 0 >$

res: T

offset: $0 < 0, 0 >$

res: T

Architecture of WasmBounds



How can we be more confident that WasmBounds does not make false positives?

Two strategies so far:

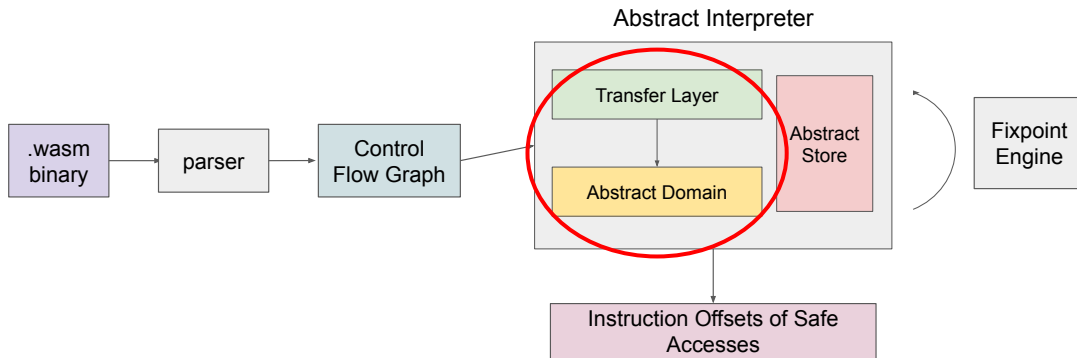
- 1) Verify the soundness of the abstract domain with Verus**
- 2) Make the transfer layer infer Wasm semantics from SpecTec**

Two strategies so far:

1) **Verify the soundness of the abstract domain with Verus**

2) **Make the transfer layer infer Wasm semantics from SpecTec**

- Similar to Mikail Khan and Ben Titzer's Canonical Bytecode Definitions



What does “soundness” of the abstract domain mean?

Operations on the abstract intervals over-approximates the corresponding operation on the associated concrete set.

For example,

- $\gamma(A) \oplus \gamma(B) \subseteq \gamma(\text{add}(A, B))$
- $\gamma(A) \cap \gamma(B) \subseteq \gamma(\text{meet}(A, B))$
- $\gamma(A) \cup \gamma(B) \subseteq \gamma(\text{join}(A, B))$
- $\text{contains}(A, B) \Rightarrow \gamma(B) \subseteq \gamma(A)$

How does Verus verify that the domain is sound?



```
pub fn join(&self, joinee: &Self) -> (result: Self)
  requires
    self.wf(),
    joinee.wf(),
  ensures
    result.wf(),
    forall|value: u32|
      self.member(value) || joinee.member(value) ==> result.member(value),
```

Extract ground truth out of SpecTec

According to the spec,

```
i32.add:  
  c1 := stack.pop()  
  c2 := stack.pop()  
  stack.push(iadd(c1, c2))
```

Replace `iadd()` with `AbstractI32::add()`

Conclusion

Abstract interpretation is a viable method for recovering safe memory accesses from a Wasm binary.

Thank you for listening!

Contact me at:

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